

Equivalence testing of complex particle size distribution  
profiles based on earth mover's distance  
Complex Generic Drug Product Development Workshop  
Session 3: Complex Formulations/Dosage Forms  
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**Meng Hu, PhD.**

Division of Quantitative Methods and Modeling,  
Office of Research and Standards  
OGD | CDER | US FDA

# Earth



# Outline

- Background
- Method
- Case study
- Conclusion

# Background

- The particle size distribution (PSD) comparisons can be a useful tool to assess equivalence between a generic product and the reference listed drug (RLD) product.
- The FDA has recommended the population bioequivalence (PBE) statistical approach on D50 and SPAN values to compare PSD of generic and RLD products when appropriate.

# Background

Recently, a new method, namely earth mover's distance (EMD), is recommended in the product-specific guidances (PSGs) for PSD analysis.

*Contains Nonbinding Recommendations*

## Draft Guidance on Cyclosporine

This draft guidance, when finalized, will represent the current thinking of the Food and Drug Administration (FDA, or the Agency) on this topic. It does not establish any rights for any person and is not binding on FDA or the public. You can use an alternative approach if it satisfies the requirements of the applicable statutes and regulations. To discuss an alternative approach, contact the Office of Generic Drugs.

**Active Ingredient:** Cyclosporine  
**Dosage Form; Route:** Emulsion; ophthalmic

**Strength:** 0.05%

**Recommended Study:** Two options: in vitro or in vivo

### I. In vitro option:

To qualify for the in vitro option for this drug product at met.

- i. The test and reference listed drug (RLD) formulation quantitatively (Q2)<sup>3</sup> the same<sup>3</sup>.
- ii. Acceptable comparative physicochemical characteristics: The comparative study should be performed

*Contains Nonbinding Recommendations*

## Draft Guidance on Barium Sulfate

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**Active Ingredient:** Barium sulfate  
**Dosage Form; Route:** For suspension; oral

**Strength:** 98% (334 g / bottle)

**Recommended Studies:** In vitro study

### Additional Comments:

- The proposed test drug product should be qualitatively (Q1)<sup>1</sup> and quantitatively (Q2)<sup>3</sup> the same as the reference listed drug (RLD).
- Test and reference drug products should have comparable physicochemical properties, including but not limited to, viscosity across a range of shear rates (e.g., low, medium, and high), and pH.
- The comparative analyses should be performed on at least three lots of the test drug product and three lots of the reference drug product.

*The EMD-based approach described in the PSG for cyclosporine ophthalmic emulsion*

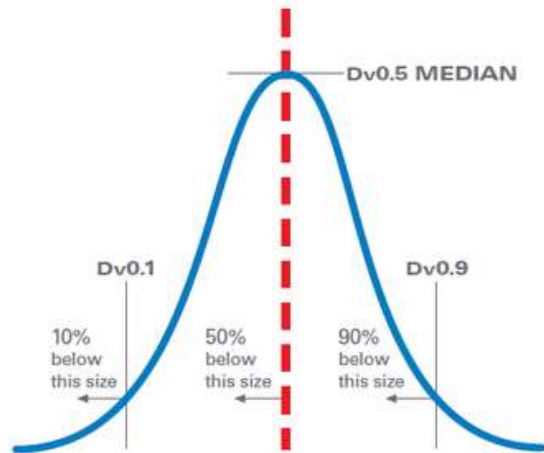
**Bioequivalence based on (95% upper confidence bound):** Considering the fact that the shape of the globule size distribution of this product may not be mono-modal, the conventional population BE based on D50 and SPAN may not be sufficient to demonstrate bioequivalence.

Instead, the equivalence between the test and RLD formulations in the shape of the globule size distribution (such as the presence of multiple peaks) should be demonstrated by a method proposed by the sponsor. A statistical metric is preferred to assess the difference (e.g., in terms of distance) between the shapes of distribution profiles. One suggested approach is the earth mover's distance (EMD)<sup>5</sup> method, which computes the minimal cost needed to transform one distribution into the other using an optimization algorithm. An average profile of all RLD samples (i.e., RLD center) is calculated and served as the reference profile to compute the distance between a RLD or a test sample to the RLD center. After obtaining the profile distances between each RLD sample and the RLD average ('RLD' – 'RLD center' distance), and the profile distances between each test sample and the RLD average ('TEST' – 'RLD center' distance), a statistical metric should be employed to quantify the difference between the two categories of distances. One suggested method is the population BE test<sup>6,7</sup>. In order to properly account for variability of the reference product and to achieve adequate power, a sufficient number of samples and replicates should be used.

# Why EMD rather than D50/SPAN?

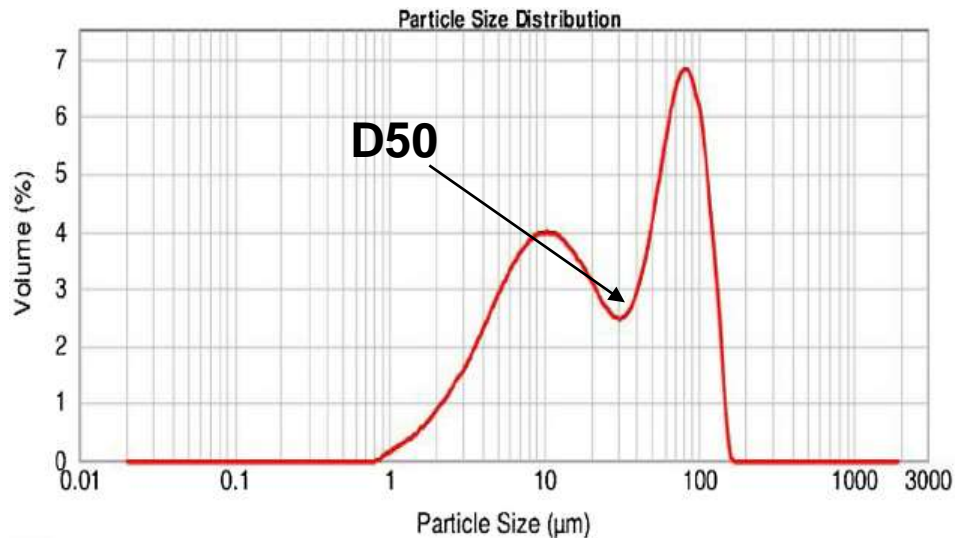
**D50: Median**

**SPAN:  $(D_{90}-D_{10})/D_{50}$**



**Mono-modal (single-peak)  
assumption is applied.**

For a complex (e.g., multimodal) PSD profile, D50 and SPAN may not be appropriate metrics for the profile analysis.

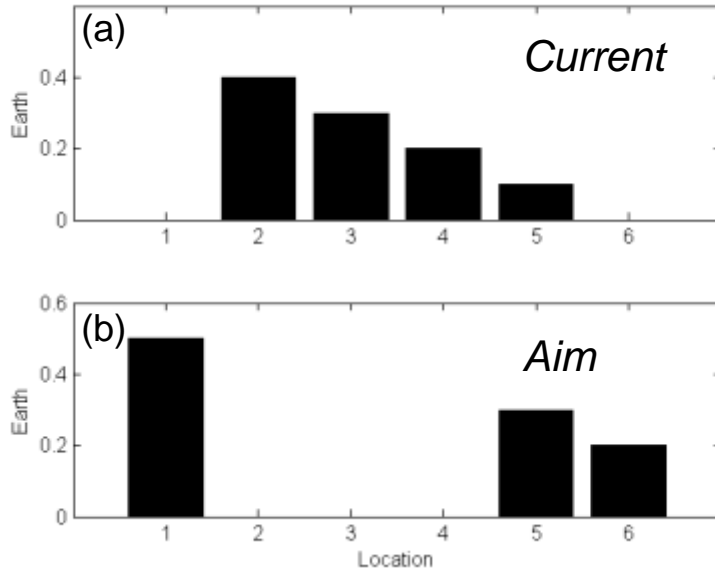


Here is the place where the **EMD** comes into play for whole profile comparison.

# What is EMD?



EMD was derived from a transportation question:



**What is the minimum cost of moving earth from the '*Current*' pile to the '*Aim*' pile?**

## Note:

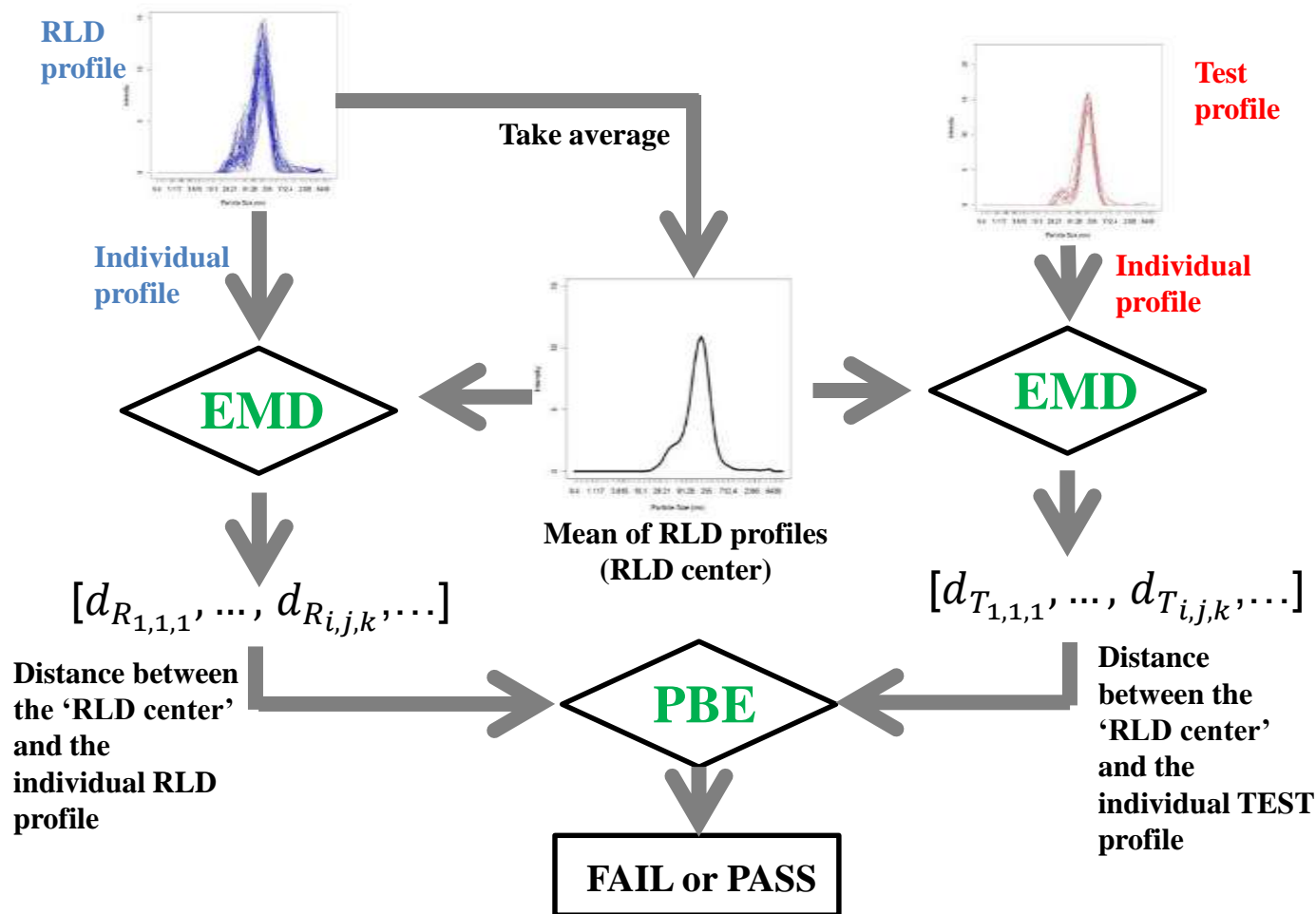
1. The cost includes 'amount of earth moved' and 'moving distance'.
2. If the earth pile is considered as histogram, the EMD can be used to assess the difference between histograms.

# EMD for profile comparison

- The EMD is a widely used tool in pattern recognition, machine learning, computer vision, etc., especially for discriminant analysis of the histogram-type data.
- PSD (intensity) is the typical histogram data.
- The EMD can be used to compare the PSD profiles for equivalence test.



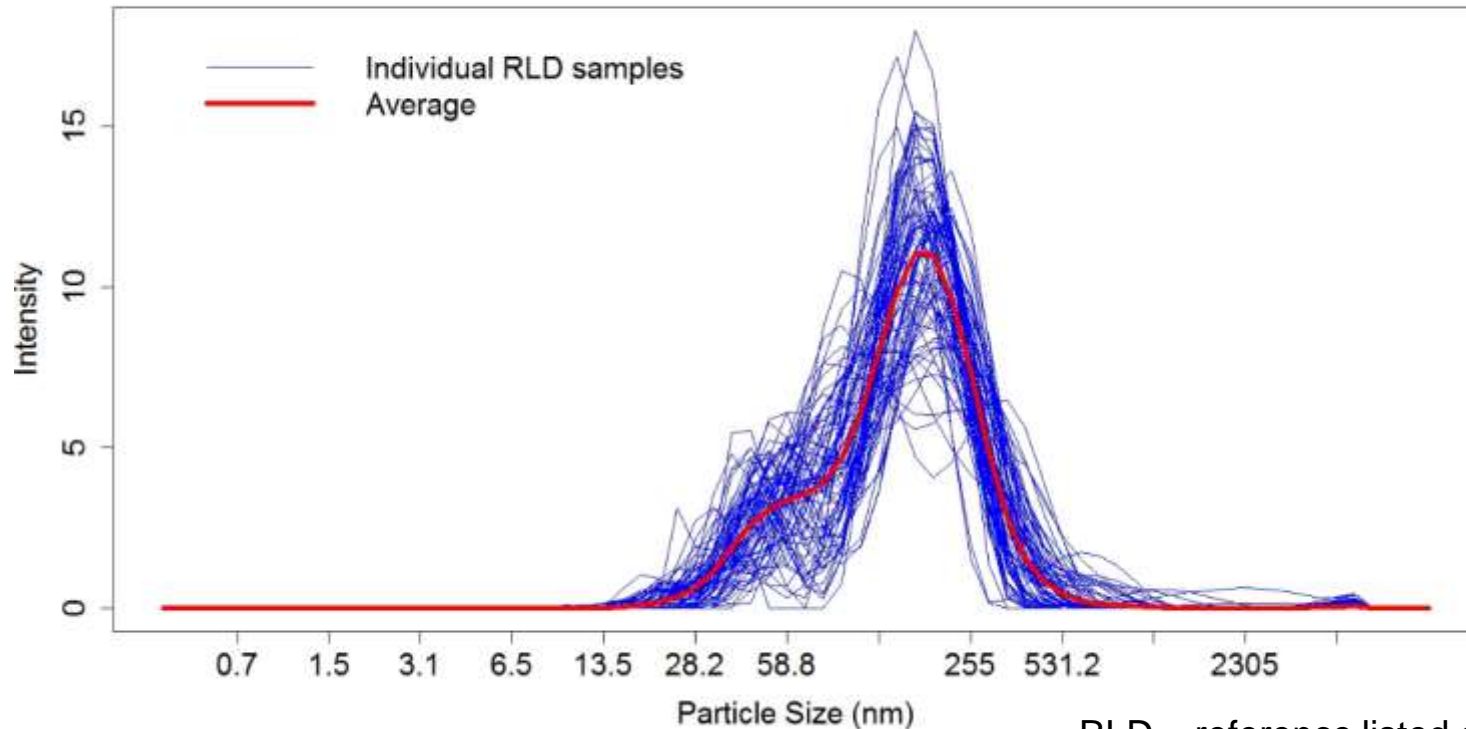
# Equivalence approach based on EMD



# Case Study - cyclosporine ophthalmic emulsion



PSD profiles from cyclosporine ophthalmic emulsion (RLD)

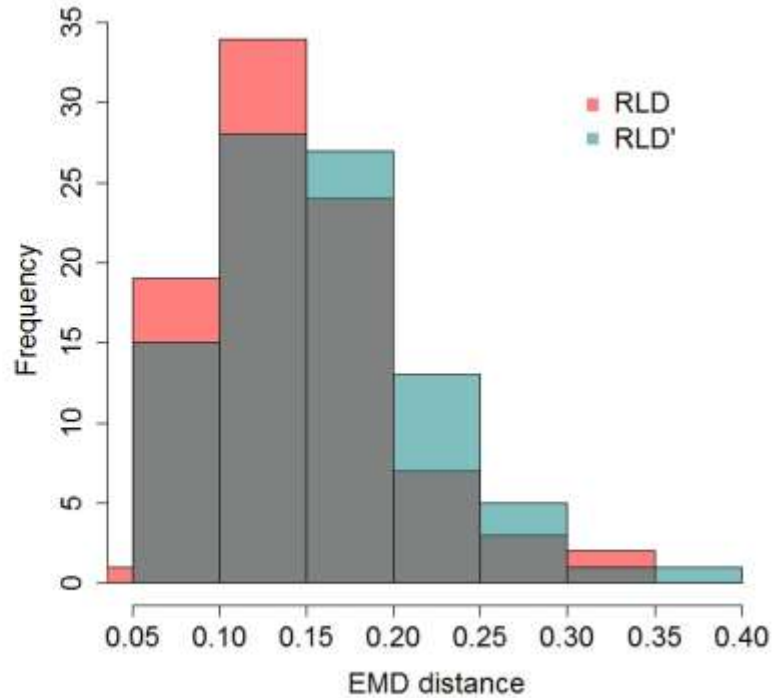
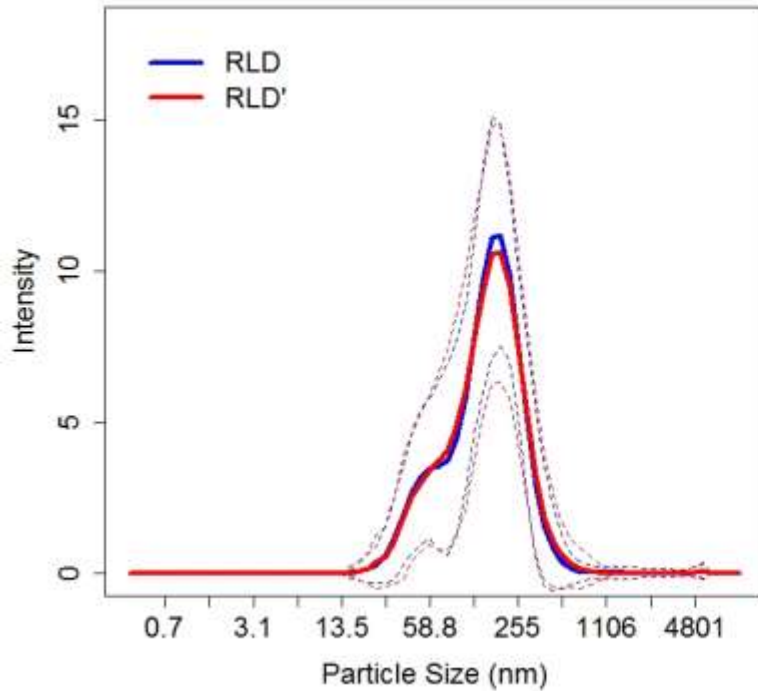


- Demonstrate the usefulness of developed approach
  - RLD vs. RLD
  - RLD vs. Negative control
  - Simulations

# Data for cyclosporine emulsion

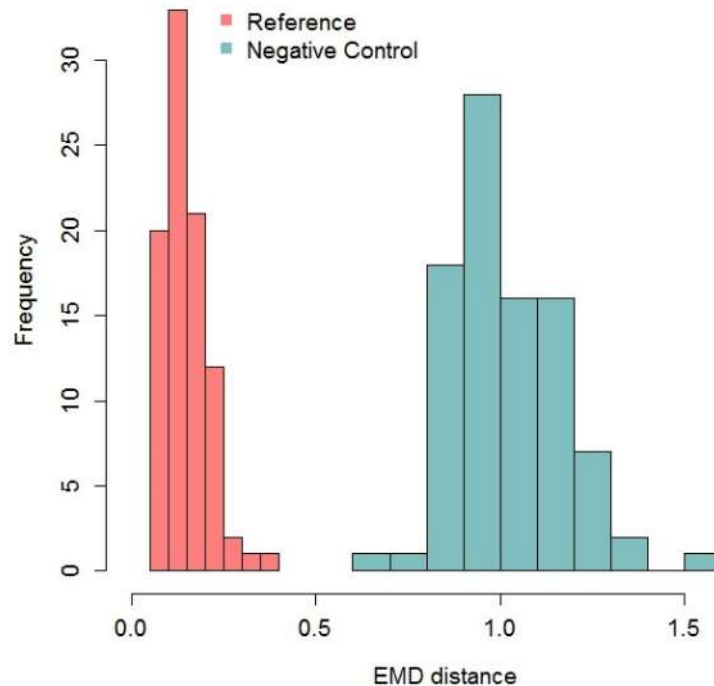
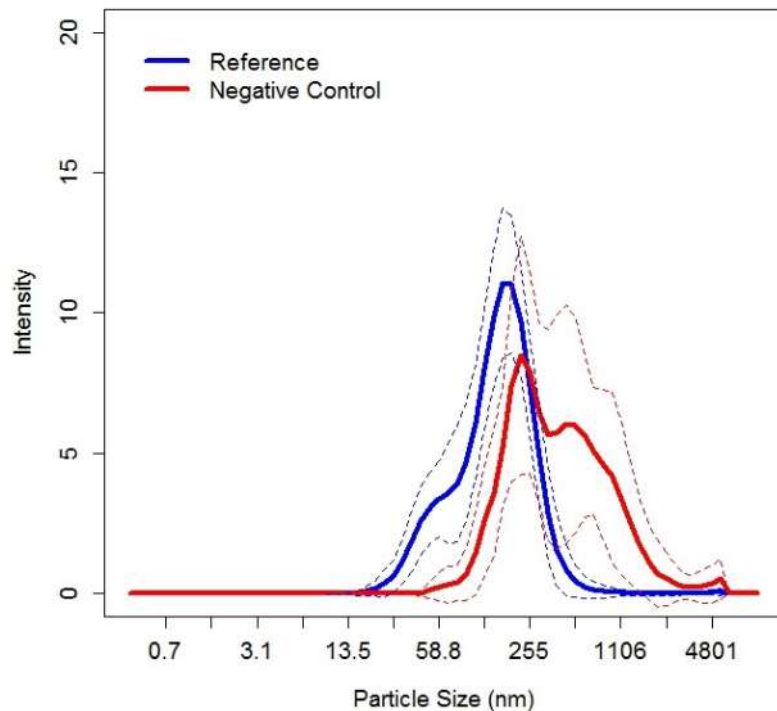
- Reference listed drug (RLD) – 8 lots
- Negative control - 3 lots

# RLD vs. RLD



The PBE is applied to the EMD distances from two groups, concluding equivalence.

# RLD vs. Negative Control



The PBE is applied to the EMD distances from two groups, concluding that equivalence can not be established.

# Simulations – performance test

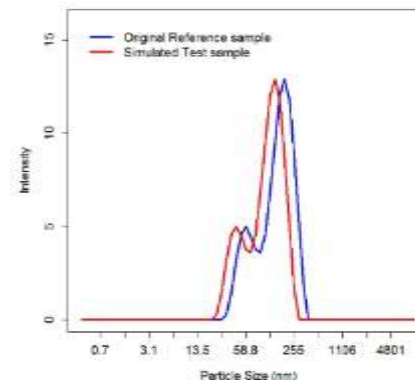
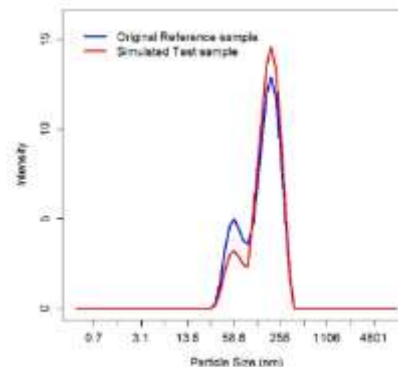
Based on real PSD profiles

Systematically changing profile

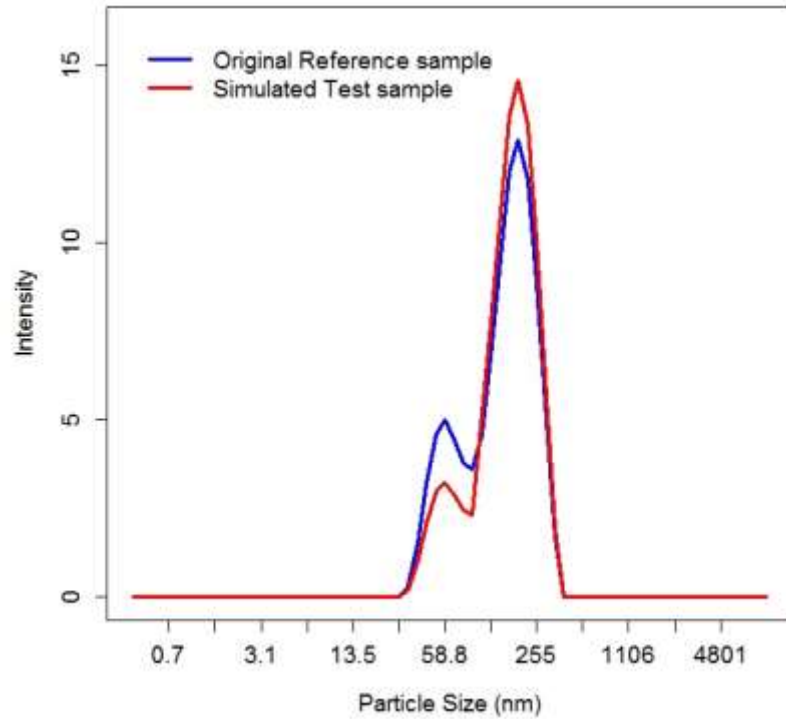
Systematically shifting Profile

Compare EMD with other distance methods

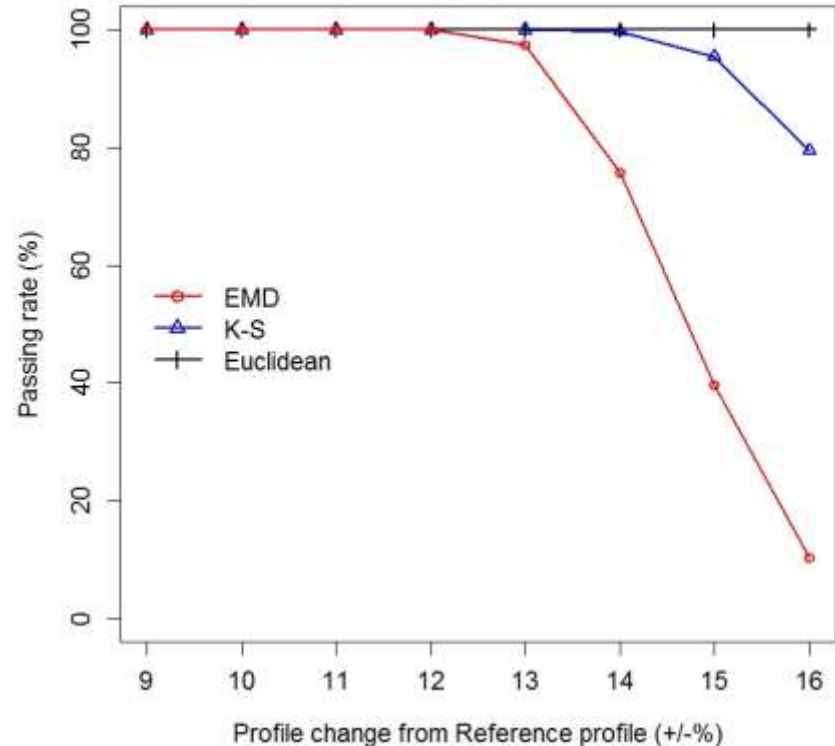
- Euclidean distance
- Kolmogorov–Smirnov (K-S) distance



# Simulations - Profile changing

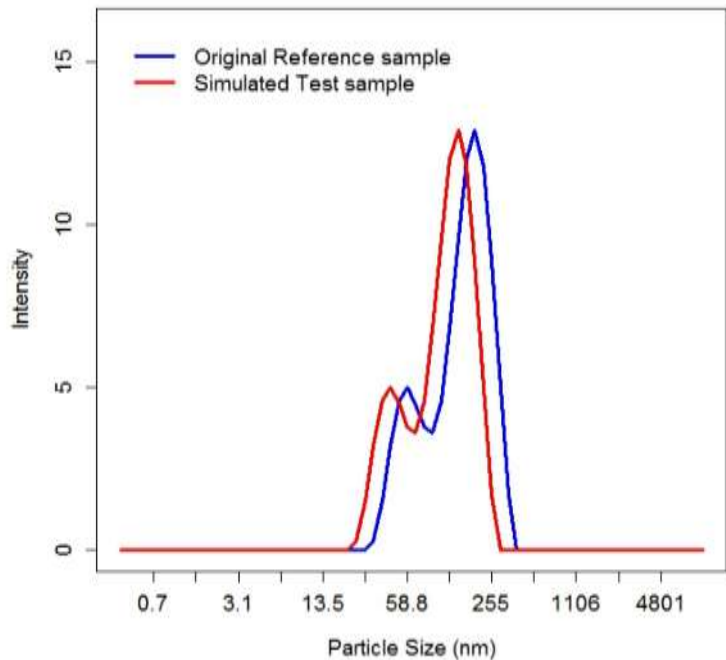


EMD-based equivalence approach provides the best sensitivity to discriminate the profile difference.





# Simulations - Profile shifting



## Passing rates (%) of equivalence tests

Number of shifted bins	Equivalence approach based on		
	EMD	K-S	Euclidean
1	100	93	100
2	0	0	100
3	0	0	47

Overall, the EMD-based approach offers the optimal performance.

# Conclusion

- An EMD-based equivalence approach can be used for the complex PSD profile comparison between a generic product and the RLD product.
- The method validations show that the EMD approach is able to effectively reject the unaccepted products (e.g., negative control), and pass the accepted products (e.g., reference itself).
- EMD has been recommended in our PSGs and been applied to the ANDA assessments.

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